

# Quantifying the Shape of a Plant (Brassica rapa) During Growth Under **Different Light Intensities Using Fractal Geometry**



Modeling Biological Phenomena

### Introduction

The process by which plants allocate resources to different structures is guided by complex underlying mechanisms. Understanding how plants adapt to stressors by varying allocation can provide important information for developing sustainable agricultural processes. The goal of this study was to be able to model and parameterize how the structure of plants changes in response to varying light intensities, from low insufficient light levels up to light levels certainly sufficient for optimal growth.

The structure of plants was captured by their fractal dimension. Fractal dimension, a measure of how objects fill space, can provide a wholistic understanding of plant shape and how that shape changes as the plants react to their environments. Std. Strain Brassica rapa are a model organism for assays into plant morphology as their quick life cycle (less than 1 month under ideal circumstances) allows for rapid experimentation. Furthermore, extensive use in scientific studies means that these plants are well understood and can provide robust, repeatable data.

## Methods

In order to obtain real fractal dimension growth curves for a plant, Std. Strain Brassica rapa were grown under three different lighting conditions over 23 days with eight replicates each. Light conditions varied based on intensity and were as follows: low (40 µEinsteins), medium (75 µEinsteins) and high (100 µEinsteins). Plants in each treatment were scanned using a NextEngine 3D Laser Scanner UHD with a resolution of 16K points/in<sup>2</sup> at 9, 12, 16, 19 and 23 days after planting. By the end of the 23 days, plants had reached the end of their growth cycle. An algorithm was developed to determine the fractal dimension of each scan using a 3d boxcounting method. The box-counting method involves determining the minimum number of cubes,  $N_{\epsilon}$ , with side length  $\epsilon$  required to completely cover the object. This process is repeated for increasingly small  $\epsilon$ . Then, a log-log plot of  $N_{\epsilon}$  vs  $1/\epsilon$  is constructed for each of these coverings and the fractal dimension, D, is defined as the slope of the data.

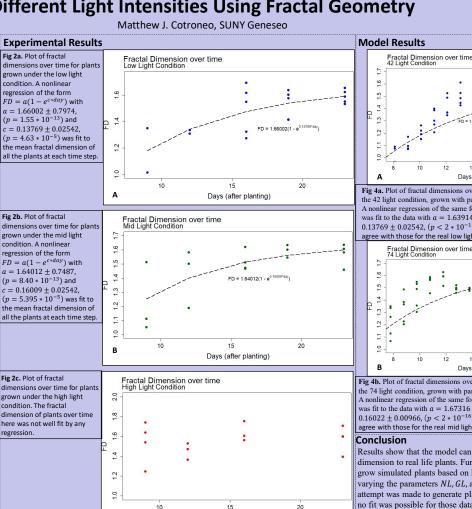
Due to the imperfect nature of the LIDAR scanner, although the overall structure of the plant is well captured, small discontinuities are sometimes present in the portion of scans representing stems and petioles (Fig. 1). As a result the log-log plot of  $N_{\epsilon}$  vs  $1/\epsilon$  is not a single linear line, but rather possesses two or three distinct slopes



Fig. 1. Four views of a (rotating by 90° between each view) 3D reconstruction of a young plant scanned . Notice that while most of the structure is well captured by the scanner, there are a few spots in thin netioles where data was not properly captured. This plant has fractal dimension D = 1.250481

depending on the range of  $1/\epsilon$  considered. In order to best capture the structure of these plants without noise from the discontinuities, D, was determined using intermediate values of  $\epsilon$ , ignoring cube counts for cubes with sides longer than

10% of the plant's height as well as cubes with sides smaller than the thickness of a petiole.

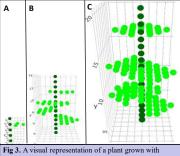


#### Model

A diffusion-limited aggregation model was developed to simulate plant growth. At the top of the simulated space, light intensity was set to 74 or 42 (out of 100) to simulate the mid and low light conditions respectively. Light intensity in each cell slightly decreases with increasing distance from the top level. Stem pieces are added vertically in a single column at a constant rate; leaf pieces, are added at each time step with probability NL, undergo a random walk from the edge of the simulated space until they attach to the stem. Leaf pieces already attached can spawn new a leaf piece horizontally adjacent to themselves with probability GL. GL is scaled by the light intensity at the existing leaf's location. Furthermore, new leaf pieces can only be added a maximum of MD cells from the stem. Each plant is allowed to grow for 14 time steps in all simulations. After time step 9, no random walk leaves are added, new leaf pieces can only be produced from existing leaf pieces. The fractal dimension for plant is calculated at each time step using the same method as for the real plants.

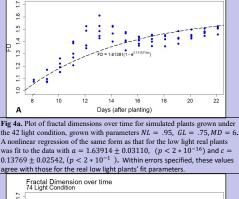
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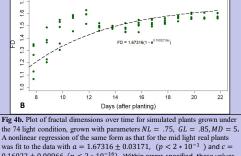
Δ



Davs (after planting)

conditions NL = 0.85, GL = 0.95, MD = 5 and light intensity 74. A: The plant at time step 2 with D = 1.0803. **B**: The plant at time step 7 with D = 1.4687. C: The plant at time step 14 with D = 1.5429.





 $0.16022 \pm 0.00966$ , ( $p < 2 * 10^{-16}$ ). Within errors specified, these values agree with those for the real mid light plants' fit parameters.

Results show that the model can generate plants with a similar fractal dimension to real life plants. Furthermore, the model can reliably grow simulated plants based on light intensity available and by varying the parameters NL, GL, and MD (Fig. 4a, Fig. 4b). No attempt was made to generate plants under the high light condition as no fit was possible for those data. Altogether, fractal dimension proves to be an effective measure of plant complexity and morphology and this model shows promise for simulating fractal dimension over time under varying parameters.

Work for future endeavors will include parameterizing the response of Brassica rapa plants to other conditions such as below ground nutrients available. Assays into the sensitivity of the model to changes in NL, GL, and MD may also reveal further information on what influences how plants adapt to available light intensity.

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#### References

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